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Abstract: Type II seesaw leptogenesis simultaneously explains the origin of neutrino masses, the baryon asym-	663.9
metry of our universe, and inflation. The Large Hadron Collider (LHC) provides an opportunity to directly test type	651.4
II seesaw leptogenesis by looking for the predicted triplet Higgs. In this paper, we perform an analysis of the detec-	638.9
tion prospect for the triplet Higgs at the LHC through multi-electron channels. We find that due to the contribution	626.4
of the $pp \rightarrow H^{\pm\pm}H^{\mp}$ process, the sensitivity of multi-electron channels searching for doubly-charged Higgs pair pro-	613.9
duction can be improved. We also investigate the $3e + E_T^{\text{miss}}$ signals to probe $pp \to H^{\pm\pm}H^{\mp}$ production and find that	601.2
the future high luminosity LHC could probe a triplet Higgs around 1.2 TeV at the $2\sigma$ level.	588.0
Keywords: type II seesaw, Triplet Higgs, LHC	569.0
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526.9	
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### I. INTRODUCTION

One of the unresolved issues in modern physics is the origin of the neutrino mass. In the standard model (SM)<sub>480.9</sub> neutrinos are massless, but observation of neutrino oscillation indicates that neutrinos have tiny masses, which requires extension of the SM. The most popular ideas for 444.9 generating neutrino masses are so-called seesaw mechan-432.9 isms, which can be classified into three types. The type 420.9 I/III seesaw introduces three (or at least two) additional 400.9 singlet/triplet fermions [1–5], whereas the type II seesaw only includes an additional triplet scalar, which provides a minimal framework to explain the origin of neutrino 372.9 masses [6-11]. In the model of the type II seesaw, the triplet Higgs can directly couple to the lepton sectors, and 448.9 if the neutral component of the triplet Higgs gets a vev, 336.9 the Majorana mass of the neutrinos can be generated. 324.9 Interestingly, the type II seesaw could also provide feasible leptogenesis if it also plays the role of inflaton, as 200.9 pointed out by a recent study [12, 13]. Therefore, this 200.9 simple model could explain three important problems at 276.9 the same time: the origin of neutrino masses, the baryon asymmetry of our universe, and inflation. Compared with 252.9 leptogenesis from the type I seesaw, which generally re-240.9 quires a high scale right-handed neutrino [14], type II<sub>228.9</sub> seesaw leptogenesis allows the triplet Higgs to be as light

as the TeV scale, which means it could be directly probed 514.9 by the Large Hadron Collider (LHC). Indeed, the LHC<sub>502.9</sub> already performs some surveys and currently sets a limit<sub>490.9</sub> of around a few hundred GeV for the doubly charged 478.9 Higgs contained in the triplet Higgs depending on its decay products [15–19]. The decay of the doubly charged 454.9 Higgs is sensitive to the vacuum expectation value of the triplet Higgs. For a large vev  $v_A \ge 0.1$  MeV, it mainly de-430.9 cays into two gauge bosons; otherwise, it decays into 418.9 dileptons [20]. However, if baryon asymmetry is gener-400.9 ated by the type II seesaw, to avoid the lepton number being washed out, a vev of the triplet Higgs  $v_A < 1$  keV is  $_{882.9}$ preferred. Therefore, looking for the triplet Higgs through the leptonic channel would provide a visible way to test type II seesaw leptogenesis. In this paper, we investigate the detection capability of the triplet Higgs in future large<sup>334,9</sup> hadron colliders. Previous studies on this aspect have been investigated in numerous works including, for example, Refs. [21–32]. A test of type II seesaw leptogenesis from lepton flavor violation can be also found in 2000 provident of the second seco [33]. 274.9

In the model of the SM with additional triplet Higgs, after electroweak symmetry breaking, besides the SM- $_{250.9}$ like Higgs there are six additional scalars present in the spectrum, which can be denoted as  $A^0$ ,  $H^0$ ,  $H^{\pm}$ ,  $H^{\pm\pm}_{26.9}$ where  $A^0$ ,  $H^0$  are the extra CP-odd/even neutral scalars,  $_{214.9}$ 

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and  $H^{\pm}, H^{\pm\pm}$  are the charged Higgs and doubly-charged 742.3 Higgs, respectively. The charged Higgs or the doubly-730.3 charged Higgs can be pair-produced through the Drell-718.3 Yan process, providing good channels to probe the triplet Higgs at the colliders. The ATLAS group already performs a search for the doubly-charged Higgs assuming it mostly decaying into dileptons, and the mass of the provident of the provi doubly-charged Higgs  $H^{\pm\pm}$  up to around 800 GeV is excluded  $[15, 17]^{1}$ . Depending on the number of observed e46.3 leptons, the detection strategy is classified mainly into [834.3 three categories: the four-lepton channel, three-lepton channel, and two-lepton channel. Each channel has different sensitivity and the final result is derived from the combination of these three channels. On the other hand, 586.3 as the triplet Higgs is a triplet under the SM  $SU(2)_{L^{574.3}}$ group, the charged Higgs can be produced together with the doubly-charged Higgs. This production rate can be even higher than the  $H^{\pm\pm}$  pair production [35]. Noticing 538.3 that the charged Higgs decays into a lepton and a neutrino, the  $H^{\pm\pm}H^{\mp}$  production can also contribute to the 514.3 ATLAS search channels and a better sensitivity can be 502.3 derived. We will demonstrate this point later. 490 3

In addition, as the charged Higgs decays into a charged lepton and a neutrino, a large missing energy is present for the  $H^{\pm \pm}H^{\mp}$  pair production. It would be intriguing to search for the  $H^{\pm \pm}H^{\mp}$  pair production via the signal of  $3e + E_T^{\text{miss}}$ , which may provide good sensitivity to the triplet Higgs. This paper is organized as follows: in the triplet Higgs. This paper is organized as follows: in the triplet Higgs. This paper is organized as follows: in the triplet Higgs. This paper is be sensitivity and the triplet Higgs model and the mechanism of type II seesaw leptogenesis. In Sec. III we calculate the production of  $H^{\pm}$  and  $H^{\pm\pm}$  at the LHC. We analysis the sensitivity of the triplet Higgs at the LHC, including the contribution of  $H^{\pm \pm}H^{\mp}$  pair production, and then we show the prospect for  $H^{\pm\pm}H^{\mp}$ searches requiring a large missing energy for the final states in Sec. V. We draw our conclusion in Sec. VI

#### II. TYPE II SEESAW MODEL

The scalar sector of type II seesaw model contains the 275.7 SM Higgs doublet  $\Phi$  and a  $SU(2)_L$  triplet scalar field  $\Delta_{P83.7}$  with hypercharge Y = 1, which can be written as

$$\Delta = \begin{pmatrix} \frac{\delta^+}{\sqrt{2}} & \delta^{++} \\ \delta^0 & -\frac{\delta^+}{\sqrt{2}} \end{pmatrix}, \qquad \Phi = \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}. \tag{1}$$

The most general renormalizable and gauge invariant Lagrangian for the scalar sector is

$$\mathcal{L} \supset \left( D_{\mu} \Phi \right)^{\dagger} D^{\mu} \Phi + \operatorname{Tr} \left( D_{\mu} \Delta \right)^{\dagger} D^{\mu} \Delta - V(\Phi, \Delta).$$
(2)

Besides SM Yukawa interaction, one can include an additional Yukawa interaction term between the triplet Higgs and leptons,

$$\mathcal{L}_{\nu} = -y_{\nu}L^{\mathrm{T}}C\,\mathrm{i}\,\sigma_{2}\Delta L + \mathrm{h.c.},\qquad(3)_{\mathrm{EF54}}$$

where the  $y_{\nu}$  is the Yukawa coupling, L is the left-handed lepton doublet, and C is the charge conjugation operator. After spontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-vanspontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and  $\Phi$  acquire a non-van-spontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  acquire a non-van-spontaneous electroweak symmetry breaking (EWSB), the neutral part of  $\Delta$  and (EWSB), the neutral part of  $\Delta$  and (EWSB) (EWSB)

$$\langle \Delta \rangle = \begin{pmatrix} 0 & 0\\ \frac{\nu_{\Delta}}{\sqrt{2}} & 0 \end{pmatrix}, \qquad \langle \Phi \rangle = \begin{pmatrix} 0\\ \frac{\nu_{\Phi}}{\sqrt{2}} \end{pmatrix}, \qquad (4)$$

where  $v_{\Delta}$  is the vacuum expectation value of the neutral part of the triplet Higgs. The neutrino mass can then be generated by

$$m_{\nu} = \sqrt{2} y_{\nu} v_{\Delta}. \tag{5}_{\text{AB1}}$$

Here,  $m_{v}$  is a complex symmetric 3×3 matrix and the physical neutrino masses can be derived by diagonalizing  $m_{v}$  with PMNS matrix U. The gauge invariant potential for the scalar sector can be written as follows:

$$V(\Phi, \Delta) = -m_{\Phi}^{2} \Phi^{\dagger} \Phi + m_{\Delta}^{2} \operatorname{Tr}(\Delta^{\dagger} \Delta)$$
  
+  $(\mu \Phi^{T} i \sigma_{2} \Delta^{\dagger} \Phi + \text{h.c.}) + \frac{\lambda}{4} (\Phi^{\dagger} \Phi)^{2}$   
+  $\lambda_{1} (\Phi^{\dagger} \Phi) \operatorname{Tr}(\Delta^{\dagger} \Delta) + \lambda_{2} [\operatorname{Tr}(\Delta^{\dagger} \Delta)]^{2}$   
+  $\lambda_{3} \operatorname{Tr}[(\Delta^{\dagger} \Delta)^{2}] + \lambda_{4} \Phi^{\dagger} \Delta \Delta^{\dagger} \Phi, \qquad (6)_{\text{seas}}$ 

where  $m_{\Phi}^2$  and  $m_{\Delta}^2$  are the mass parameters and the  $\mu$  term<sup>504,8</sup> provides a source of lepton number violation. The  $\mu$  term<sup>202,4</sup> violates lepton number two units for the lepton number<sup>200,4</sup> assignments of  $l_{\Delta} = -2, l_{\Phi} = 0.$ 

After electroweak symmetry breaking we have a state of doubly-charged Higgs  $H^{\pm\pm} (\equiv \delta^{\pm\pm})$ , two states of charged scalars  $H^{\pm}$  and  $G^{\pm}$ , which are combinations of  $\delta^{\pm}$  and  $\phi^{\pm}$ , and the *CP*-even neutral states  $H^0$ ,  $h^0$  as well as the *CP*-odd states  $A^0$ ,  $G^0$ , where  $G^{\pm}$  and  $G^0$  are the Goldstone bosons, which will ultimately give the longitudinal degrees of freedom of the  $W^{\pm}$  and Z bosons. The mass-squared of the doubly-charged Higgs is given as

$$m_{H^{\pm\pm}}^2 = \frac{\sqrt{2\mu}v_{\Phi}^2 - 2\lambda_3 v_{\Delta}^3 - \lambda_4 v_{\Phi}^2 v_{\Delta}}{2v_{\Delta}}.$$
 (7)

551183.4

89.1

287.9375

293 7

The mass-squared of the charged Higgs is

$$m_{H^{\pm}}^{2} = \frac{2\sqrt{2}\mu v_{\Phi}^{2} + 4\sqrt{2}\mu v_{\Delta}^{2} - \lambda_{4}v_{\Delta}v_{\Phi}^{2} - 2\lambda_{4}v_{\Delta}^{3}}{4v_{\Delta}}.$$
 (8)

742.3

80.3

For the mass of the CP-even/odd scalars, one can obtain: 578

$$m_{H^0}^2 = \frac{1}{2} [A + C + \sqrt{(A - C)^2 + 4B^2}], \qquad (9)$$

$$m_{h^0}^2 = \frac{1}{2} [A + C - \sqrt{(A - C)^2 + 4B^2}], \qquad (10)$$

$$m_{A^0}^2 = \frac{\mu \left( v_{\Phi}^2 + 4 v_{\Delta}^2 \right)}{\sqrt{2} v_{\Delta}},\tag{11}$$

where

$$A = \frac{\lambda}{2} v_{\Phi}^{2}, \quad B = -\sqrt{2}\mu v_{\Phi} + (\lambda_{1} + \lambda_{4})v_{\Phi}v_{\Delta},$$
$$C = \frac{\sqrt{2}\mu v_{\Phi}^{2} + 4(\lambda_{1} + \lambda_{4})v_{\Delta}^{3}}{2v_{\Delta}}.$$
(12)

In the limit of  $v_{\Delta} \ll v_{\Phi}$ , we have the following mass relation of the physical eigenstates:

$$m_{H^{\pm\pm}}^2 - m_{H^{\pm}}^2 \approx m_{H^{\pm}}^2 - m_{H^0/A^0}^2 \approx -\frac{\lambda_4 v_{\Phi}^2}{4}.$$
 (13)

One can define the mass-splitting parameter  $\Delta m = \frac{1}{9543}$   $m_{H^{\pm\pm}} - m_{H^{\pm}}$  which describes the typical mass difference of  $\frac{1}{9423}$ the spectra for the triplet Higgs sector. The decay behavi- $\frac{1}{3903}$ or of the triplet Higgs is different from different paramet- $\frac{1}{3183}$ er spaces [20, 30, 31, 36]. For  $\Delta m < O(10)$  GeV and  $\frac{1}{9063}$   $v_{\Delta} < 10^{-4}$  GeV, the  $H^{\pm\pm}/H^{\pm}$  decays into  $l^{\pm\pm}/l^{\pm}v$ . For  $\frac{1}{943}$   $\Delta m < O(10)$  GeV and  $v_{\Delta} > 10^{-4}$  GeV,  $H^{\pm\pm}/H^{\pm}$  decays in  $\frac{1}{2922}$ to  $W^{\pm\pm}/W^{\pm}Z$  or  $W^{\pm}h^{0}$ . If  $\Delta m > O(10)$  GeV, the cascade  $\frac{1}{701}$ decay channels become significant. In the case of triplet  $\frac{1}{29461}$ keV [37], and thus the  $H^{\pm\pm}/H^{\pm}$  would mainly decay into  $\frac{1}{29461}$ LHC. In the following we briefly discuss how to achieve  $\frac{1}{2961}$ 

#### A. Leptogenesis through type II seesaw

It is known that the minimal type II seesaw model cannot successfully lead to thermal leptogenesis, and thus the Affleck-Dine mechanism is considered. In the Afffleck-Dine mechanism, the scalar field acquires a large vev along the flat direction during the inflationary epoch. nonzero baryon or lepton number, the baryon or lepton number violating interactions induce a rotating trajectory for the vev, which can generate baryon or lepton asymmetry and transfer to ordinary particles at the end of inflation. Fortunately, the Affleck-Dine mechanism can be achieved in the minimal type II seesaw model.

Considering the non-minimal couplings of  $\Delta$  and  $\Phi$  to gravity, the relevant Lagrangian in the Jordan frame can be written as

$$\frac{\mathcal{L}}{\sqrt{-g}} \supset -\frac{1}{2}M_P^2 R - f(\Phi, \Delta)R + g^{\mu\nu}(D_\mu \Phi)^{\dagger}(D_\nu \Phi) + g^{\mu\nu} \text{Tr}(D_\mu \Delta)^{\dagger}(D_\nu \Delta) - V(\Phi, \Delta), \qquad (14)_{\text{BF7.2}}$$

where *R* is the Ricci scalar. To simplify the analysis, we focus on the neutral components  $\phi^0$  and  $\delta^0$  and considered the non-minimal coupling to be

$$f(\Phi, \Delta) = \xi_{\Phi} |\phi^{0}|^{2} + \xi_{\Delta} |\delta^{0}|^{2}.$$
(15)

Through a Weyl transformation, the Lagrangian can be written in the Einstein frame, in which the gravitational portion is of Einstein-Hilbert form. It can be shown that the scalar potential in the Einstein frame is

$$V_E(\Phi, \Delta) = \frac{M_P^4}{\left(M_P^2 + 2f(\Phi, \Delta)\right)^2} V(\Phi, \Delta),$$
(16)

which exhibits a flat direction at the large field limit of  $\phi^{0}_{80.8}$ and  $\delta^{0}$ . This flat direction can be recognized as a Starobinsky-like inflationary trajectory, and the inflaton is the mixing of  $\delta^{0}$  and  $\phi^{0}$ .

As the triplet  $\Delta$  carry lepton number  $I_{\Delta} = -2$  and the  $\mu_{3223}^{3323}$  term induces lepton number violating interaction, all the  $\mu_{323}^{3323}$  ingredients of Affleck-Dine mechanism are included. <sup>3083</sup> During the inflationary evolution, the non-trivial motion <sup>2063</sup> of the angular direction of  $\delta^0$  can generate lepton number <sup>2063</sup> asymmetry, which transfers to ordinary particles during <sup>2723</sup> reheating. After reheating, a part of the net lepton num-<sup>2063</sup> ber is converted to baryon number through the sphaleron <sup>2483</sup> process.

However, if any lepton number violating processes  $^{24.3}$  are in thermal equilibrium after reheating, the generated  $^{212.3}$  lepton asymmetry will be washed out. We require that the  $^{200.3}$  processes  $LL \leftrightarrow HH$  and  $HH \leftrightarrow \Lambda$  are never in thermal  $^{180.3}$  equilibrium:  $^{76.3}$ 

$$\Gamma|_{T=m_{\Delta}} = n \langle \sigma v \rangle \approx y^2 \mu^2 / m_{\Delta} < H|_{T=m_{\Delta}}, \qquad (17)$$

$$\Gamma_{ID}(HH \leftrightarrow \Delta)|_{T=m_{\Delta}} \simeq \frac{\mu^2}{32\pi m_{\Delta}} < H|_{T=m_{\Delta}}, \qquad (18)$$

176.1

where 
$$H|_{T=m_{\Delta}} = \sqrt{\frac{\pi^2 g_*}{90} \frac{m_{\Delta}^2}{M_p}}$$
. Using  $v_{\Delta} \simeq -\frac{\mu v_{\rm EW}^2}{2m_{\Delta}^2}$  and Eq. (18), the necessary condition to avoid the washout effect resolution to be

$$v_{\Delta} \lesssim 10^{-5} \text{ GeV} \left(\frac{m_{\Delta}}{1 \text{ TeV}}\right)^{-1/2}$$
. (19)

96.6

307.3625

093104-4

For  $m_{\Delta} \gtrsim 1$  TeV, we require that  $v_{\Delta} \lesssim 10$  keV to prevent the washout effect and achieve successful leptogenesis.

# **III. PRODUCTION AND DECAY OF THE** TRIPLET HIGGS

The triplet Higgs can be produced at the LHC by the neutral current and charged current Drell-Yan process, 566.6

$$\begin{aligned} q\bar{q} \stackrel{\gamma^{*}/Z^{*}}{\longrightarrow} H^{\pm\pm} H^{\mp\mp}/H^{\pm}H^{\mp}/H^{0}A^{0}, \\ q\bar{q}' \stackrel{W^{*}}{\longrightarrow} H^{\pm\pm}H^{\mp}/H^{\pm}H^{0}/H^{\pm}A^{0} \end{aligned}$$

and the Feynman diagrams for  $H^{\pm\pm}H^{\mp\mp}$ ,  $H^{\pm\pm}H^{\mp}$  production are presented in Fig. 1.

$$q(p_1) + \bar{q}(p_2) \to H^{++}(k_1) + H^{--}(k_2),$$
  
 $q(p_1) + \bar{q}'(p_2) \to H^{++}(k_1) + H^{-}(k_2).$ 

The parton level cross section at leading order (LO) for 402.7 these processes are:

$$\frac{d\sigma}{dy}(q\bar{q} \to H^{++}H^{--})$$

$$=\frac{3\pi\alpha^{2}\beta_{1}^{3}(1-y^{2})}{N_{c}s}\left\{e_{q}^{2}+\frac{s}{(s-M_{Z}^{2})^{2}}\frac{\cos 2\theta_{W}}{\sin^{2}2\theta_{W}}\right\}, \quad (20)$$

$$\times\left[4e_{q}g_{V}^{q}(s-M_{Z}^{2})+4(g_{V}^{q}+g_{A}^{q})s\frac{\cos 2\theta_{W}}{\sin^{2}2\theta_{W}}\right]\right\}, \quad (20)$$

$$NH: BR(H^{++} \to \mu\mu), BR(H^{++} \to \tau)$$

$$\frac{d\sigma}{dy}(q\bar{q}' \to H^{++}H^{-}) = \frac{\pi\alpha^{2}\beta_{2}^{3}(1-y^{2})}{16N_{c}\sin^{4}\theta_{W}}\frac{s}{(s-M_{W}^{2})^{2}}, \quad (21)$$

$$IH: BR(H^{++} \to ee) \gg BR(H^{++} \to \mu)$$

$$IH: BR(H^{++} \to ee) \to H^{++} \to \mu$$

$$IH: BR(H^{++} \to ee) \to \mu$$

$$IH: BR(H^{++} \to ee)$$

where  $y = p_1 \cdot k_1$ , s is the partonic center-of-mass energy,  $r_{42.3}$ and  $\alpha$  is the QED coupling evaluated at the scale  $\sqrt{s}$ .  $e_{\alpha}$ is the electric charge of the quark q.  $\beta_1 = \sqrt{1 - 4m_{H^{**}}^2/s_{\gamma^{15.7}}}$  $\beta_2 = \sqrt{(1 - (m_{\pm} + m_{H^{\pm\pm}})^2/s)(1 - (m_{\pm} - m_{H^{\pm\pm}})^2/s)}.$ In Fig. 2 we show the cross section of  $H^{\pm\pm}H^{\mp\mp}$ ,  $H^{\pm}H^{\mp}, H^{\pm\pm}H^{\mp}$  pair production with a varying mass of the triplet Higgs. We consider a K-factor of 1.25 [38] for Fig. 664.9 2, and we assume  $H^{\pm\pm}$ ,  $H^{\pm}$  share the same mass parameter. The doubly-charged triplet Higgs has a considerable cross section and a distinctive decay signature, the samecharge lepton final state. Note that  $H^{\pm\pm}H^{\mp}$  has an even larger cross section than  $H^{\pm\pm}H^{\mp\mp}$  production, and thus may provide a better sensitivity of triplet Higgs search. 592.9

The decay modes of triplet Higgs with different  $v_{\Lambda} - \Delta m$  parameters have been thoroughly discussed in 568.9 Refs. [20, 30, 31, 36]. We consider  $\Delta m < O(1)$  GeV and 566.9  $v_{\Delta} < 10^{-6}$  GeV, and thus the doubly-charged Higgs  $H^{\pm\pm}_{544.9}$ and singly-charged scalars mostly decay to leptonic final 532.8 states. The decay branching ratios are given by

$$BR(H^{\pm\pm} \to l_i^{\pm} l_j^{\pm}) = \frac{2}{1 + \delta_{ij}} \frac{\left| y_{ij}^{\nu} \right|^2}{\sum_{mn} \left| y_{mn}^{\nu} \right|^2}, \qquad (22)$$

$$BR(H^{\pm} \to l_i^{\pm} v_j) = \frac{|y_{ij}|^2}{\sum_{mn} |y_{mn}|^2},$$
(23)

 $\frac{1}{\sqrt{2\nu_{\Delta}}} U \operatorname{diag}(m_1, m_2, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_2, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_2, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_2, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname{diag}(m_1, m_3) U^{\mathrm{T}} \text{ and } y = \frac{\cos\beta}{\nu_{\Delta}} \operatorname$ with  $y_{\nu} =$ scillation experiments. The leptonic 370.9 b depends on the mass order of the 358.9 the neutrino mass spectrum. It has 346.9 normal hierarchy (NH) and inverted<sub>334.9</sub> 22.9

$$\begin{split} \mathrm{NH} &: \mathrm{BR}(H^{++} \to \mu\mu), \mathrm{BR}(H^{++} \to \tau\tau) \gg \mathrm{BR}(H^{++} \to ee), \\ \mathrm{IH} &: \mathrm{BR}(H^{++} \to ee) \gg \mathrm{BR}(H^{++} \to \mu\mu), \mathrm{BR}(H^{++} \to \tau\tau). \end{split}$$

ume BR $(H^{++} \rightarrow ee) = 100\%$  to present<sub>246.2</sub>

 $l^{+}(l^{+})$ 

 $l^+(\overline{v}_l)$ 

 $l^{-}(l^{-})$ 



## **IV. MULTIELECTRON SEARCHES AT THE LHC** 517.4

The ATLAS collaboration has released a multilepton final state search with an integrated luminosity of 487.4 36.1 fb<sup>-1</sup> of pp collisions at  $\sqrt{s} = 13$  TeV [17]. This ana-475.4 lysis focuses on the decays  $H^{\pm\pm} \rightarrow e^{\pm}e^{\pm}, H^{\pm\pm} \rightarrow e^{\pm}\mu^{\pm}, \text{ or}_{463.1}$  $H^{\pm\pm} \rightarrow \mu^{\pm}\mu^{\pm}$  with a branching ratio around 100%. The events are divided into three signal regions. Their selection criteria are shown in Table 1. The final state events with 2, 3 electrons are also considered due to the missing 415.1 electrons in the detector. In this study, we first simulate the experimental process by adding the contribution of point  $H^{\pm\pm}H^{\mp}$  to the signal event because it also contributes the area to the signal event because it also contributes the area to the signal event because it also contributes the state of the signal event because it also contributes the state of the signal event because it also contributes the state of the signal event because it also contributes the state of the s 2,3 electron signal region. In our simulation, we implement the triplet Higgs model in FeynRules [39], and import UFO files [40] into MadGraph [41] to generate signal events. We use the NNPDF23LO1 [42] for parton distribution function and the parton showering and hadronization are simulated with PYTHIA8 [43]. We perform the approximate the perform the perform the perform the perform the perform the performance of t detector simulations with Delphes [44] and data analysis with ROOT [45].

For the two-electron and three-electron signal regions (SR2E and SR3E), at least one pair of electrons with the same charge is required. The separation of the samecharge electrons and the scalar sum of the electron trans-28.1

			.1 . 1	
Table 1. Selec	tion criter	ria in all	the signal	regions.

		<u> </u>	
	SR2E	SR3E	SR4E
<i>b</i> -jet veto	0	0	0
Z veto		0	o
$P_T\left(e^{\pm}e^{\pm}\right) > 100 \text{ GeV}$	0	0	
$\sum  P_T(e)  > 300 \text{ GeV}$	0	0	
$\Delta R\left(e^{\pm},e^{\pm}\right) < 3.5$	0	0	
$\Delta M/ar{M}$			0

verse momenta are required to be  $\Delta R(e^{\pm}e^{\pm}) > 3.5$  and  $T_{42.3}$  $\sum |P_T(e)| > 300$  GeV, respectively. The vector sum of the 729.7 electron transverse momenta is required to be 717.7  $P_T(e^{\pm}e^{\pm}) > 100$  GeV. The selection criteria for electrons<sup>705.3</sup> are  $|\eta| < 2.47$  and  $P_T > 30$  GeV. Besides the pre-selection 692.8 cut described above, for the signal regions SR3E and SR4E, events are rejected if any opposite-charge sameflavor electron pair is within 10 GeV of the Z boson mass to reduce the background from Z production. In the four- $_{B44.8}$ electron signal region (SR4E), there must be two elec-632.8 tron pairs with the same charge and the total charge is [520.8 zero. The  $\Delta M/\bar{M}$  requirement is applied to exclude the source background where the two same-charge pairs have ininvariant masses  $(\Delta M = |m^{++} - m|, _{584.4})$ compatible  $\frac{m^{++}+m}{2}$ ). In the ATLAS experiment, for different 4665.9  $\overline{M} =$ the value of  $\Delta M$  is different. We simply take  $\overline{M},$  $\Delta M/\bar{M} < 0.1$  in the four-electron channel. In all signal re-538.6 gions, the invariant masses of same-charge electron pairs 526.5 are required to be above 200 GeV. In order to restrain 514.5 background events arising from top-quark decays, events 502.5 with *b*-tagged jets are vetoed. To validate our simulation, we first simulate the sig-478.5

To validate our simulation, we first simulate the signal events from  $pp \rightarrow H^{\pm\pm}H^{\mp\mp}$  production and obtain the signal cut efficiency. Using the observed signal event from the article, we apply the *CLs* method [46] to obtain the 95% CL upper limits on the  $pp \rightarrow H^{\pm\pm}H^{\mp\mp}$  cross section. The result is shown in Fig. 3, denoted as the black dashed curve [17]. As a comparison, the limit from the ATLAS experiment is also shown as the black dotted line. It shows our limit is close to the one derived from the ATLAS experiment.

As  $pp \rightarrow H^{\pm\pm}H^{\mp}$  contributes the SR2E and SR3E signal regions, we expect the real limit should be stronger.346.5 Therefore, we simulate the process  $pp \rightarrow H^{\pm\pm}H^{\mp} \rightarrow_{334.5}$  $l^{\pm}l^{\pm}l^{\mp}\nu^{\pm}$  and obtain the corresponding signal efficiency. To combine our results, we denote  $\sigma_{1,2}$  and  $\varepsilon_{1,2}$  as the state  $\sigma_{1,2}$  and  $\varepsilon_{1,2}$  as the state  $\sigma_{1,2}$  and  $\sigma_{1,2}$  as the state  $\sigma_{1,2}$  and  $\sigma_{1,2}$  cross section and cut efficiency for the  $pp \rightarrow H^{\pm\pm}H^{\mp\mp}_{2^{99.5}}$ process and  $pp \rightarrow H^{\pm\pm}H^{\mp}$  process, respectively, and then the total signal events  $n = \mathcal{L}\sigma_1\varepsilon_1 + \mathcal{L}\sigma_2\varepsilon_2$  for each signal  $\sigma_{1,2,5}$ region. We set the limit on the total signal events. Tope25 show our results, we can use an effective cut efficiency of  $\varepsilon_{\text{2eff}} = \varepsilon_2 + \sigma_1 / \sigma_2 \varepsilon_1$  for the  $pp \to H^{\pm \pm} H^{\mp}$  process and set the limit on the cross section of  $pp \rightarrow H^{\pm\pm}H^{\mp}$  production, which is shown as the red dashed curve in Fig. 3. It 14.14.5 shows the combined limit is around 100 GeV stronger 1025 than the one derived only from the  $pp \rightarrow H^{\pm\pm}H^{\mp\mp}$  process

## **V.** $3e + E_T^{\text{miss}}$ SIGNAL

Note that  $pp \rightarrow H^{\pm\pm}H^{\mp}$  has a larger cross section and the final states include a missing energy. It is intriguing to examine whether  $3e + E_T^{\text{miss}}$  could provide a better sensitivity to the triplet Higgs.

50 5





**Fig. 3.** (color online) Limits for  $B(ee)/B(e\mu)/B(\mu\mu) = 100\%/$  0%/0%. The black and red solid lines represent the production cross sections of the  $pp \rightarrow H^{\pm\pm}H^{\mp\mp}$  and  $pp \rightarrow H^{\pm\pm}H^{\mp}$  processes, respectively. The black dashed line is the 95% CL limit we obtain for the  $pp \rightarrow H^{\pm\pm}H^{\mp\mp}$  process, which is comparable to the limit obtained by ATLAS and depicted as a black dotted line. The red dashed line is the 95% CL limit we obtain by adding the contributions of the two processes together.

The relevant background for this signal mainly originates from diboson (*ZZ*, *ZW*, *WW*),  $t\bar{t}$ ,  $t\bar{t}W$ ,  $t\bar{t}Z$ ,  $t\bar{t}h$ , triboson and Drell-Yan processes. However, as shown in the ATLAS paper, for the 3/ process, the diboson background is much more dominant than the other backgrounds. Therefore for the background simulation, we use only consider the events from the diboson process. The background and the signal are both simulated by using MadGraph with an MLM matching. For the cross section NLO correction. The LO cross-section for the diboson process and the corresponding *K*-factor at  $\sqrt{s} = 13$  TeV LHC [47] are shown in Table 2.

To ensure simulation credibility and validate the share misidentification effect in the electron channel, the same-charge region (SCR) is also considered, which and exerts b-jet veto. For  $pp \rightarrow H^{\pm\pm}H^{\mp} \rightarrow l^{\pm}l^{\pm}l^{\mp}v^{\pm}$ , large missing transverse energy appears in the final states. We show the missing energy distribution of the diboson process and  $pp \rightarrow H^{\pm\pm}H^{\mp} \rightarrow l^{\pm}l^{\pm}l^{\mp}v^{\pm}$  process in Fig. 4. It shows that a cut on the missing energy around a few hunand decomposition of the background.

The distinction of the missing energy distribution  $_{2073}$  between the signal and diboson background motivates us to add a missing energy cut  $E_T^{miss} > 300$  GeV. The cut  $_{1832}$ 

Table 2.LO cross sections and K-factors for diboson pro-duction at  $\sqrt{s} = 13$  TeV.141

	s = 15 TeV.				_141
	ZZ	$W^+Z$	$W^-Z$	WW	1
$\sigma_{ m LO}/ m pb$	9.89	15.51	9.53	67.74	
K-factor	1.62	1.84	1.91	1.66	

flow for the background and signal for a luminosity 742.3 3000 fb<sup>-1</sup> at 13 TeV LHC are shown in Table 3. It clearly 730.3 shows that only 10% of the background is left after im-718.3 posing the cut  $E_T^{\text{miss}} > 300 \text{ GeV}$ , whereas most of the signal events are still kept. Using expected discovery significance S /  $\sqrt{B}$ , the results are shown in Fig. 5 at 13 TeV<sub>B817</sub> LHC with luminosity 3000 fb<sup>-1</sup>. We find a triplet mass less than 1.2 TeV can be reached at  $2\sigma$  for the high luminosity LHC in the future. As a comparison, we also [545.3 show the  $2\sigma$  sensitivity for the multi-electron searches 633.3 channels mentioned in last section where the missing energy cut is not imposed. We find that when the triplet Higgs mass is below 800 GeV, the multi-electron channel still provides better sensitivity for the triplet Higgs. However, the  $3e + E_T^{\text{miss}}$  signal could reach a higher triplet 4732Higgs mass when the triplet Higgs mass is larger than 800 GeV. The main reason for this is that when the mass



**Fig. 4.** (color online) Missing transverse energy distribution of the  $pp \rightarrow H^{\pm\pm}H^{\mp} \rightarrow l^{\pm}l^{\pm}l^{\mp}\nu^{\pm}$  (*B*(*ee*) = 100%) process and diboson background with the pre-selection. The masses of  $H^{\pm\pm}$ ,  $H^{\mp}$  are assumed to be 1 TeV here.

<b>Table 3.</b> Cut flow for the diboson background and the sign	- 242.3
nal $(m_{H^{++}} = 600 \text{ GeV} m_{H^{++}} = 900 \text{ GeV} m_{H^{++}} = 1200 \text{ GeV}$	) 230 -
with an integrated luminosity of 3000 fb <sup>-1</sup> and $\sqrt{s} = 13$ TeV	218

	Diboson BKG	600 GeV	900 GeV	1200 GeV
Pre-selection	14518	2249	242	38
$m_{\rm invariant} > 200 { m GeV}$	3037	2199	241	38
$P_T\left(e^{\pm}e^{\pm}\right) > 100 \text{ GeV}$	1379	2168	239	37
$\sum  P_T(e)  > 300 \text{ GeV}$	673	2139	237	37
$\Delta R\left(e^{\pm}, e^{\pm}\right) < 3.5$	490	1596	174	26
$E_T^{\text{miss}} > 300 \text{ GeV}$	49.1	790	111	20
Significance	-	113	15.8	2.9



of the triplet Higgs is low, the missing energy could be lower and the missing energy cut could also hurt the signal. We believe that an even larger missing energy cut could further suppress the background and a better sensitivity for the heavy triplet Higgs can be reached.

### **VI. CONCLUSION**

Type II seesaw leptogenesis simultaneously explains<sup>449.0</sup> the origin of neutrino masses, the baryon asymmetry of 437.0 our universe, and inflation. The LHC provides an oppor-425.0 tunity to directly test type II seesaw leptogenesis by look-4130 ing for the predicted triplet Higgs. In this paper, we per-401.0 form an analysis of the detection prospect for the triplet Higgs at the LHC through multi-electron channels. Wearro find that due to the contribution of the  $pp \rightarrow H^{\pm\pm}H^{\mp}$  process, the sensitivity of multi-electron channels searching for the doubly-charged Higgs pair production can be im-pato proved. We also investigate the  $3e + E_T^{\text{miss}}$  signals to probe proved. the  $pp \rightarrow H^{\pm\pm}H^{\mp}$  production and we find this channel<sub>316.4</sub> may provide better sensitivity than the multi-electron<sup>304.4</sup> channels. Our results show that the future LHC could<sup>292.4</sup> probe a triplet Higgs around 1.2 TeV at the  $2\sigma$  level with a luminosity of 3000 fb<sup>-1</sup> for the  $3e + E_T^{\text{miss}}$  search channel.

### APPENDIX A. THE CL<sub>s</sub> METHOD

Indistinguishable from background hypotheses in the case of few signal events, we use the  $CL_s$  method to improve experimental sensitivity. The usual confidence level for signal and background hypothesis is given by 173.9 the probability that the test-statistic Q is less than or equal to the value observed in the experiment:

$$CL_{s+b} = P_{s+b}(Q \le Q_{\text{obs}}) = \int_{-\infty}^{Q_{\text{obs}}} \frac{\mathrm{d}P_{s+b}}{\mathrm{d}Q} \mathrm{d}Q, \qquad (A1)$$

where  $\frac{dP_{s+b}}{dQ}$  is the probability distribution function for signal and background experiments. Likewise, the confidence level in the background-only hypothesis is:

$$CL_b = P_b(Q \le Q_{\text{obs}}) = \int_{-\infty}^{Q_{\text{obs}}} \frac{\mathrm{d}P_b}{\mathrm{d}Q} \mathrm{d}Q, \qquad (A2)_{\text{sec}}$$

and  $\frac{dP_b}{dQ}$  is the probability distribution function for background-only experiments.

To obtain the limit, we use the definition of  $CL_s$ 

$$CL_s = \frac{CL_{s+b}}{CL_b}.$$
 (A3)

The signal hypotheses is excluded at the confidence level

$$1 - CL_s \le CL. \tag{A4}_{429}$$

To combine the results of the signals from several chan-

$$Q = \prod_{i=1}^{n} q_i \tag{A5}$$

with

$$q_{i} = \frac{\frac{e^{-(s_{i}+b_{i})}((s_{i}+b_{i})^{N_{i}}}{N!}}{\frac{e^{-b_{i}}b_{i}^{N_{i}}}{N!}}$$
(A6)

for counting experiments. The estimated signal and back- $_{27.1}$  ground are  $s_i$  and  $b_i$ , respectively, and *i* labels the chan- $_{226.1}$  nel. *N* is the number of observed candidates. The final  $_{213.1}$  likelihood function should also include the uncertainty of  $_{201.1}$  the backgrounds. All of the above calculations can be  $_{189.1}$  preformed numerically by the Monte Carlo method.  $_{77.1}$ 

References	743.8	[26] <sub>743.8</sub> P. S. Bhupal Dev and Y. Zhang, JHEP 10, 199 (2018), 743.8
		arXiv:1808.00943 733.3
[1] <sub>723.3</sub> P. Minkowski, Phys. Lett. B 67, 421 (1977)	723.3	[27]7228 T. B. de Melo, F. S. Queiroz, and Y. Villamizar, Int. J. 722.8
[2]7128 T. Yanagida, Conf. Proc. C 7902131 95 (1979)	712.8	Mod. Phys. A 34, 1950157 (2019), arXiv:1909.07429
[3]7023 S. L. Glashow, NATO Sci. Ser. B 61 687 (1980)	702.3	[28]7018 R. Primulando, J. Julio, and P. Uttayarat, JHEP 08, 024701.8
[4]601.8 M. Gell-Mann, P. Ramond, and R. Slansky, Conf. Proc. C	691.8	(2019), arXiv:1903.02493
<b>790927</b> , 315 (1979), arXiv:1306.4669	681.3	[29]680.8 R. Padhan, D. Das, M. Mitra <i>et al.</i> , Phys. Rev. D 101,680.8
[5]670.8 R. Foot, H. Lew, X. G. He et al., Z. Phys. C 44, 441 (1989)	670.8	075050 (2020), arXiv:1909.10495
[6]660.3 M. Magg and C. Wetterich, Phys. Lett. B 94, 61 (1980)	660.3	[30] 659.8 S. Ashanujjaman and K. Ghosh, JHEP 03, 195 (2022), 659.8
[7] <sub>649.8</sub> T. P. Cheng and LF. Li, Phys. Rev. D 22, 2860 (1980)	649.8	arXiv:2108.10952 649.3
[8]639.3 G. Lazarides, Q. Shafi, and C. Wetterich, Nucl. Phys. B	639.3	[31]6388 S. Mandal, O. G. Miranda, G. Sanchez Garcia <i>et al.</i> , Phys. 638.8
<b>181</b> , 287 (1981)	628.8	Rev. D 105, 095020 (2022), arXiv:2203.06362
[9]618.3 R. N. Mohapatra and G. Senjanovic, Phys. Rev. D 23, 165	618.3	[32]6178 L. Duarte, V. P. Goncalves, D. E. Martins et al., Phys. Rev. 617.8
(1981)	607.8	D 107, 035010 (2023), arXiv:2208.07599
[10] <sub>597.3</sub> J. Schechter and J. W. F. Valle, Phys. Rev. D 22, 2227	597.3	[33]596.8 N. D. Barrie and S. T. Petcov, JHEP 01, 001 (2023), 596.8
(1980)	586.8	arXiv:2210.02110 586.3
[11] <sub>576.3</sub> J. Schechter and J. W. F. Valle, Phys. Rev. D 25, 774	576.3	[34] 575.8 ATLAS collaboration, <i>Search for doubly charged Higgs</i> 575.8
(1982)	565.8	boson production in multi-lepton final states using 139 fb 1665.3
[12]555.3 N. D. Barrie, C. Han, and H. Murayama, Phys. Rev. Lett.	555.3	of proton-proton collisions at $\sqrt{s} = 13$ TeV with the ATLAS <sub>554.2</sub>
<b>128</b> , 141801 (2022), arXiv:2106.03381	544.8	<i>detector</i> , arXiv: 2211.07505 543.1
13 <sub>534.3</sub> N. D. Barrie, C. Han, and H. Murayama, JHEP 05, 160	534.3	[35]5326 A. G. Akeroyd and M. Aoki, Phys. Rev. D 72, 035011 532.6
(2022), arXiv:2204.08202	523.8	(2005), arXiv:hep-ph/0506176
14 <sub>5133</sub> G. F. Giudice, A. Notari, M. Raidal <i>et al.</i> , Nucl. Phys. B	513.3	[36]5116 M. Aoki, S. Kanemura and K. Yagyu, Phys. Rev. D 85,511.6
<b>685</b> , 89 (2004), arXiv:hep-ph/0310123	502.8	055007 (2012), arXiv:1110.4625
15]4923 CMS collaboration, A search for doubly-charged Higgs	492.3	[37] <sub>490.6</sub> C. Han, S. Huang, and Z. Lei, Phys. Rev. D 107, 015021 <sub>490.6</sub>
boson production in three and jour lepton final states at	481.8	(2023), arXiv:2208.11336
$\frac{\sqrt{s}=13 \text{ fev}}{160}$	470.7	$[38]_{469.6}$ M. Muhlleitner and M. Spira, Phys. Rev. D 68, 117/01 <sub>469.6</sub>
$[16]_{459.6}$ A. M. Sirunyan <i>et al.</i> (CMS collaboration), Phys. Rev. Lett.	459.6	(2003), arXiv:hep-ph/0305288
120, 081801 (2018), arXIV:1709.05822	449.1	[39]448.6 A. Alloul, N. D. Christensen, C. Degrande <i>et al.</i> , Comput.448.6
[17] <sub>4386</sub> M. Aaboud <i>et al.</i> (ATLAS collaboration), Eur. Phys. J. C	438.6	Phys. Commun. 185, 2250 (2014), arXiv:1310.1921 438.1
(101  M  Ashered at  nL (ATLAS callebourtise) For Disc. L C	428.1	[40]427.6 C. Degrande, C. Duhr, B. Fuks <i>et al.</i> , Comput. Phys. 427.6
$[13]_{417.6}$ M. Addoud <i>et al.</i> (ATLAS collaboration), Eur. Phys. J. C 70, 58 (2010), arXiv:1808.01800	417.6	Commun. 183, 1201 (2012) 417.1
[10] G And at al. (ATLAS collaboration) [HED 06, 146 (2021)]	407.1	$[41]_{406.6}$ J. AIWall, K. Frederix, S. Frixione <i>et al.</i> , JHEP <b>07</b> , 079 <sub>406.6</sub>
arYiw 2101 11061	396.6	[42] B D Pall at al (NNDDE collaboration) [HED 04 040
[20] arch P. Fileviez Pérez, T. Han, G. Huang et al. Phys. Rev. D 78	386.1	(2015) arXiv:1410.8849
$[20]_{358}$ 1. Theve 2 rec2, 1. Hall, O. Huang <i>et ut.</i> , rigs. (ev. 1270, 015018 (2008))	3/5.0	[43] and S Ask I B Christiansen et al Computered
[21] <sub>3546</sub> P Fileviez Perez T Han G -Y Huang <i>et al</i> Phys Rev D	354.6	Phys Commun <b>191</b> 159 (2015) arXiv:1410 3012
78 071301 (2008)  arXiv 0803 3450	344.0	$[44]_{2428}$ L de Favereau C Delaere <i>et al</i> (DELPHES 3)
[22] <sub>336</sub> A Alloul M Frank B Fuks <i>et al</i> Phys Rev D 88	333.6	collaboration) IHEP 02, 057 (2014) arXiv:1307,6346
075004 (2013), arXiv:1307.1711	323.1	[45] <sub>3226</sub> R Brun and F Rademakers Nucl Instrum Meth A <b>389</b> <sub>3226</sub>
[23] <sub>3126</sub> ZL. Han, R. Ding, and Y. Liao, Phys. Rev. D 92, 033014	312.6	81 (1997)
(2015), arXiv:1506.08996	302.1	[46] <sub>3016</sub> T. Junk, Nucl. Instrum, Meth. A <b>434</b> , 435 (1999), 2016
[24]2916 ZL. Han, R. Ding, and Y. Liao, Phys. Rev. D 91, 093006	291.6	arXiv:hep-ex/9902006
(2015), arXiv:1502.05242	281.1	[47]2806 J. M. Campbell, R. K. Ellis, and C. Williams, JHEP 07, 0182806
[25]270.6 Y. Du, A. Dunbrack, M. J. Ramsey-Musolf et al., JHEP 01,	270.6	(2011), arXiv:1105.0020 270.1
101 (2019), arXiv:1810.09450	260.1	